

Detection of Stego Images by using Suspicion Value (special reference to Concentrating Stego Algorithms)

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Abstract:- The technique of concealing secret messages in the image which only the sender and intended recipient can know of, unsuspected by everyone else is called Image Steganography. This Technique is frequently used by Terrorists and criminal organizations for secure communication, dead-dropping and information exchange over internet in broad daylight. Hence, its the most preferred tool for achieving the 3 critical aspects Confidentiality, Integrity and Availability of the communication network capable of penetrating deep inside the civilian population. Identification of Images containing hidden Information is a challenging task due to lack of Efficient Algorithms, High rates of False Alarms and most importantly due to the High Computation Costs involved in Analyzing the Images. In this paper a mathematical algorithm which has a fast computation speed is designed for analyzing any stego-image generated using Spatial Domain Steganographic Algorithms and assigning it a Suspicion Value. Here Suspicion Value is a number associated with the image which is bigger for those tailored images (stego-images) which contain information and smaller for untailored images. Based on this Value it can be decided whether the given image must be interrogated thoroughly or not, further if needed thorough interrogation can be done (which requires large amount of computation time but is reliable and conclusively identifies the hidden information using various steganalytic techniques). This algorithm can be used for filtering of the suspicious images flowing through the web servers, routers, layer three switches and any other electronic media. Based on this algorithm the suspicion values of various cover and stego-images generated by three different steganographic algorithms are computed and evaluated. All the graphs and tables are generated using MATLAB ©Image Processing Tool Box.

Index Terms—Bit Plane Slicing, Cyber Crime, Distributing Steganographic Algorithms, Global Terrorism, Image Steganalysis, Multicolor LSB Transform, Pixel Aberration, SDT based Image Steganography, Suspicion Value.

1. INTRODUCTION

Image based steganography is a dangerous technique of concealing secret messages in the image in such a way that it remains unsuspected by anyone else apart from the sender and intended recipient. This technique strives to hide the very presence of the message itself from the observer, as if the message is invisible. As a result it has been used more frequently by various criminal and terrorist organizations than anybody else.[1][2][3] Various agencies even claim that 9/11 attacks have been masterminded and planned using this very technique.[4] Image Steganography has numerous advantages (desired by terrorists) like Anonymity, Electronic Dead Dropping, Secure Broadcasting and above all very high Confidentiality and Security (explained in detail in Section 5.2.1 of [5]). This makes every digital image of any Web Portal, Online Auction Site or even a Social Networking Site in all probability a malicious image (containing deadly terrorist plan or any other significant criminal data). Steganalysis is the technique of identifying such malicious Stego-images (original image which is used for hiding data is called the Cover-Image whereas the image

obtained after inserting the Secret Data into it is called Stego Image) from the bulk of innocent images. The next step of steganalysis involves either the extraction of the hidden information or corruption of the data by adding visually imperceptible noise in the image or can also be used as counter-operation tactics against the terrorists. The immense volume of images that flows throughout the internet causes problems for identification of stego-images, the cost and time required for the steganalysis of each and every image is atrocious not to mention the amount of computation required. This calls for a method which identifies any image (as malicious or not) based on its Steganographic signature.

Every steganographic algorithms has a different signature. As mentioned in [7][8] the most spatial domain steganographic algorithms can be broadly classified in to two types- Distributing Steganographic Algorithms and Concentrating Steganographic Algorithms. In other words all spatial domain steganographic algorithms either embeds the information in the Least Significant Bits of the pixel or changes the entire color code of the pixel by inserting information in more than 2 bits of the pixel. In former algorithms large number of pixels are required for inserting information because only one or two LSB is available from every pixel and hence known as

Distributing Type while in the latter algorithm the entire information can be stored in very few pixels because large numbers of bits are available from every pixel for storing information and hence called as Concentrating Type.

Since the Suspicion Value related with the Distributing Steganographic algorithms (Termed as Distributing *Suspicion Value* and represented by Λ) is already calculated in [8]. So in this paper the suspicion value related with the Concentrating Steganographic algorithms is being determined. This suspicion value (related with concentrating stego algorithms) is here onwards termed as Concentrating Suspicion Value and represented by Γ in this entire paper. Based on this suspicion value (i.e. concentrating suspicion value Γ) calculated in this paper and the distributing suspicion value Λ (determined in [8][9]) an overall suspicion value ζ for any given image is calculated. This overall suspicion value ζ for any image is the holistic measure of the presence of information hidden using any Spatial Domain Stego Algorithm (i.e. Concentrating as well as Distributing algorithms) in the image and is termed as Spatial Domain Suspicion Value and represented here by as ζ in this entire paper.

2. PRELIMINARIES FOR DETERMINATION OF CONCENTRATING SUSPICION VALUE (Γ)

The fast mathematical stego-identifier algorithm designed in this paper analyses any given digital image (for the presence of Concentrating spatial domain steganographic signatures) and quickly generates a Numerical Value (called in this text as Concentrating Suspicion Value and denoted by Γ) corresponding to every image it has analyzed. This Suspicion Value is a number which is greater for those images which are more likely to have stego information and lower for innocent images.

2.1 Preliminaries and Definition

Before we proceed to the technique of generating the Concentrating Suspicion Value Γ for any image we have to mathematically define the preliminary concepts to be used in this model. These preliminary concepts are derived from the concepts mentioned in [6] and [7].

Definition 1 (Image)

Every digital image is collection of discrete picture elements or pixels. Let M be any digital image with N pixels. So any particular pixel of image M is represented as $M(z)$ and z can be any value from 1 to N . This $M(z)$ can be a gray level intensity of the pixel in gray scale image or RGB or YCbCr value of the pixel in a color Image. The the individual RGB components of the pixel $M(z)$ in image M is represented as $M^R(z)$, $M^G(z)$ and $M^B(z)$ respectively.

Thus $M(z)$ can be a set $\{ M^R(z), M^G(z), M^B(z) \}$ or equivalent gray scale representation or $(M^R(z) + M^G(z) + M^B(z))/3$. But it is always better to consider each R, G and B components individually because the averaging effect cause loss of vital steganographic information. Further $\langle \{M\}, m \rangle$ is multiset of Image M such that $M(z) \in \{M\}$ for every $z = 1$ to N and m is a vector corresponding to the occurrence or count of every element $M(z)$ in $\{M\}$. Mathematically an image M with N pixels is explained in (1)

For any Image M with N pixels

$M(z)$ represents its pixels $\forall z : 1 \leq z \leq N$

$M(z) = \{M^R(z), M^G(z), M^B(z)\}$

or

$M(z) = (M^R(z) + M^G(z) + M^B(z))/3$

$\{M\} = \{M(z) : z=1 \text{ to } N\}$

*$m = \text{occurrence of any particular } M(z) \in \{M\}$
 $\langle \{M\}, m \rangle$ is multiset representing image M*

(1)

Definition 2 (Cardinality or Size of Image)

Any Image M consists of certain number of pixels. So any particular pixel of image M is represented as $M(z)$ and z can be any value from 1 to total number of pixels in the image. The cardinality or the size of the image M is the total number of pixels present in the image and represented as $n(M)$. So any Image M has $n(M)$ pixels.

$$M = \bigcup_{z=1}^{n(M)} M(z) \quad (2)$$

Definition 3 (Component of an Image)

Any sub part of an Image is a component of the image. In other words any Image M can be broken down into pixel groups (or clusters) and each such cluster forms a component of the image and is identified by its unique set of pixels. Thus in a Image M the Pixels $M(z)$ from $z = 1$ to $n(M)$ are the elements of the image M and the subsets of the image M are composed of some of those pixels ($M(z)$ from $z = 1$ to $n(M)$) and thus forms the components of the image. Thus if the image M is broken in to K components then any component M^i of the image M is mathematically explained as:

$M^i \subset M$ and $\forall i: 1 \leq i \leq K$

$$M = \bigcup_{\substack{M^i \subset M \\ \forall i: 1 \leq i \leq K}} M^i \quad (3)$$

Also for every component M^i of the image M the $M^i(z)$ represents the pixels of the component M^i and $n(M^i)$ represents the number of pixels in M^i .

Definition 4 (Neighborhood or Locality of Pixel)

If $\ell(M(z))$ is said to be set of neighboring pixels of any pixel $M(z)$ in image M . Then any $n_i \in \ell(M(z))$ will be such that $d(n_i, M(z)) \leq \lambda$ where d is a function which calculates distance (can be Euclidean, City-Block, Chess Board or any other type depending upon the steganographic algorithm) between its inputs (ie n_i and $M(z)$) and λ is measurement of degree of neighbourhood and should be minimum (Generally equal to 1 pixel) but also depends upon the steganographic algorithm used. Mathematically this can be represented as:

$$\ell(M(z)) = \{M(x) : M(x) \in M \text{ and } d(M(x), M(z)) \leq \lambda\} \quad (4)$$

In Fig 1 an arbitrary pixel Y is shown with its immediate neighbors P, Q, R, S, T, U, V and W . We represent this pixel Y as \dot{Y} in mathematical notation. Thus $\ell(\dot{Y}) = \{P, Q, R, S, T, U, V, W\}$ is set of neighboring pixels of pixel Y . Here $\lambda = 1$ and distance function d calculates Chess Board Distance.

P	Q	R
S	Y	T
U	V	W

Fig 1 Pixel Y

Definition 5 (Adjacent Neighbors of Pixel)

Set of Adjacent Neighbors of a pixel $M(z)$ is given as $\mathcal{A}(M(z))$. Thus $\mathcal{A}(M(z))$ is a collection of set $\{M(x), M(y)\}$ such that $M(x) \in \ell(M(z))$ and $M(y) \in \ell(M(z))$ and they are adjacent i.e $d(M(x), M(y)) = 1$ where d is a function which calculates distance. Mathematically:

$$\mathcal{A}(M(z)) = \{\{M(x), M(y)\} : M(x) \in \ell(M(z)) \text{ and } M(y) \in \ell(M(z)) \text{ and } d(M(x), M(y)) = 1\} \quad (5)$$

In Fig 1 for an arbitrary pixel Y with $\ell(\dot{Y}) = \{P, Q, R, S, T, U, V, W\}$ the $\mathcal{A}(\dot{Y}) = \{\{P, Q\}, \{Q, R\}, \{R, T\}, \{T, W\}, \{W, V\}, \{V, U\}, \{U, S\}, \{S, P\}\}$.

Definition 6 (Pixel Aberration)

Pixel Aberration of any Pixel $M(z)$ is the measure of the degree of difference of the given pixel $M(z)$ from its immediate neighborhood i.e. $\ell(M(z))$: $d \Leftrightarrow$

Chess Board Distance $\wedge \lambda=1$ (immediate neighborhood is obtained when Neighborhood or Locality Function $\ell(M(z))$ is calculated with $\lambda = 1$ and distance function d is used for determining Chess Board Distance) and represented as $\delta(M(z), \ell(M(z)))$. It is measured in terms of Standard Deviation of $\ell(M(z))$ and acts like a quantifier which gives the idea of the amount of deviation of the pixel from its immediate neighborhood.

Basic concept used for determining the pixel aberration of any pixel is based on the fact that, in any natural image a pixel $M(z)$ is expected to be as much different from its immediate neighborhood i.e. $\ell(M(z))$ as the adjacent pairs of pixels in $\ell(M(z))$ themselves are. The same concept is explained in (6).

Using simple statistical techniques the concept developed in (6) is applied for determining the value of Pixel Aberration for any Pixel in any given image. For any pixel $M(z)$ in image M the mean of its absolute difference from its immediate neighborhood $\ell(M(z))$ is given as $\overline{(M(z), \ell(M(z)))}$. And the set representing the absolute differences of the adjacent neighbors of $M(z)$ among themselves is given as $\mathcal{D}(\mathcal{A}(M(z)))$. The mean of the values of $\mathcal{D}(\mathcal{A}(M(z)))$ is given as $\overline{\mathcal{D}(\mathcal{A}(M(z)))}$ and Standard Deviation of the values of $\mathcal{D}(\mathcal{A}(M(z)))$ is given as $\sigma(\mathcal{D}(\mathcal{A}(M(z))))$. Since $M(z)$ is also a immediate neighbor of every pixel in $\ell(M(z))$ so $\overline{(M(z), \ell(M(z)))}$ must be within the limits of standard deviation of $\mathcal{D}(\mathcal{A}(M(z)))$ (represented as $\sigma(\mathcal{D}(\mathcal{A}(M(z))))$) and mean of $\mathcal{D}(\mathcal{A}(M(z)))$ (represented as $\overline{\mathcal{D}(\mathcal{A}(M(z)))}$). This degree of deviation of $M(z)$ from its neighbors $\ell(M(z))$ in terms of $\sigma(\mathcal{D}(\mathcal{A}(M(z))))$ and $\overline{\mathcal{D}(\mathcal{A}(M(z)))}$ is quantified as pixel aberration of pixel $M(z)$ and represented as $\delta(M(z), \ell(M(z)))$.

Concept of Pixel Aberration is based on the fact that:

Any pixel $M(z)$ is as much different from $\ell(M(z))$ as the pixel pairs in $\ell(M(z))$ themselves are.

Here $\ell(M(z))$ represents Immediate Neighborhood and is given as: $\ell(M(z))$; $d \Leftrightarrow$ Chess Board Distance $\wedge \lambda=1$

Thus

$$|M(z) - p| = |r - s| \text{ where } p \in \ell(M(z)) \text{ and } \{r, s\} \in \ell(M(z))$$

(6)

In terms of Fig 1 the mean of the differences of pixel Y with its neighbors i.e. elements of $\ell(\dot{Y})$ is given as $Y-P, Y-Q, Y-R, Y-S, Y-T, Y-U, Y-V$ and $Y-W$

and should be close to the differences of the adjacent pixels in $\ell(\dot{Y})$ or in other words the difference of the pixel pairs in $\mathcal{A}(\dot{Y})$ i.e. difference of the elements of the pixel pairs $\{P,Q\}$, $\{Q,R\}$, $\{R,T\}$, $\{T,W\}$, $\{W,V\}$, $\{V,U\}$, $\{U,S\}$ and $\{S,P\}$ or simply $P-Q$, $Q-R$, $R-T$, $T-W$, $W-V$, $V-U$, $U-S$ and $S-P$. Thus $(\overline{\ell(\dot{Y})}, \ell(\dot{Y}))$ is mean of modulus of $Y-P$, $Y-Q$, $Y-R$, $Y-S$, $Y-T$, $Y-U$, $Y-V$ and $Y-W$ and $\mathcal{D}(\mathcal{A}(\dot{Y})) = \{\text{modulus of } P-Q, Q-R, R-T, T-W, W-V, V-U, U-S \text{ and } S-P\}$. So aberration in pixel Y with respect to its neighborhood $\ell(\dot{Y})$ given as $\delta(\dot{Y}, \ell(\dot{Y}))$ should be within the limits of standard deviation of $\mathcal{D}(\mathcal{A}(\dot{Y}))$ and its mean $D(\mathcal{A}(\dot{Y}))$. Mathematically it is explained in (7).

$$\overline{\ell(\dot{Y})} = \frac{1}{n(\ell(\dot{Y}))} \sum_{p \in \ell(\dot{Y})} |p - Y|$$

$$\mathcal{D}(\mathcal{A}(\dot{Y})) = \{|x - y| : (x, y) \in \mathcal{A}(\dot{Y})\}$$

$$\delta(\dot{Y}, \ell(\dot{Y})) = \frac{\overline{\ell(\dot{Y})} - D(\mathcal{A}(\dot{Y}))}{\sigma(\mathcal{D}(\mathcal{A}(\dot{Y})))} \quad (7)$$

Definition 7 (Pixel Aberration of the Entire Image (Weighted Mean))

In any image M with N pixels (i.e. $n(M) = N$) the Pixel aberration of image M is given as $\delta(M)$. It is a quantifier whose high values for any given image M indicates that relatively large number of pixels in M have high pixel aberration. It is calculated by determining the weighted mean of the modulus of the pixel aberrations of the pixels of the entire image M .

Since for any image M the $\delta(M(z), \ell(M(z)))$ is the measure of deviation of $M(z)$ from its neighborhood $\ell(M(z))$ in terms of standard deviation so majority of pixels have this values located close to zero and approximately more than 68% of the pixels have pixel aberration within ± 1 (as per 3 Sigma or 68-95-99.7 rule of Statistics). Hence the simple mean of $\delta(M(z), \ell(M(z)))$ is very close to zero and is insignificantly small for all images. Since by pixel aberration analysis we have to identify those images which have larger pixel aberrations so as a remedy very small weights are assigned to less deviated values (majority of pixels which have low pixel aberration values) and larger weights are assigned to more deviated values (few counted pixels have large pixel aberrations). Thus value of $\delta(M)$ for the Image M with N pixels is given as:

$$\delta(M) = \frac{\sum_{z=1}^N |\delta(M(z), \ell(M(z)))| \times W(z)}{\sum_{z=1}^N W(z)} \quad (8)$$

Where the weight $W(z)$ for the pixel $M(z)$ is very small for majority of the pixels (which have $\delta(M(z), \ell(M(z)))$ value close to the mean value of the pixel aberration of all the pixels together in the image) and quite large for the pixels having highly deviated values of $\delta(M(z), \ell(M(z)))$ (The value of $\delta(M(z), \ell(M(z)))$ for such pixels is very different from the mean of $\delta(M(z), \ell(M(z)))$ for all pixels together). Such weights (which are larger for pixels having greater pixel aberration (in absolute terms) and much smaller for pixels having lesser pixel aberration) can be computed by taking cube of the value of pixel aberration in terms of the standard deviation. In other words the weight $W(z)$ for any Pixel $M(z)$ in image M is given as

$$W(z) = \left| \frac{\delta(M(z), \ell(M(z))) - \text{MEAN}_{z=1}^N(\delta(M(z), \ell(M(z))))}{\text{STD}_{z=1}^N(\delta(M(z), \ell(M(z))))} \right|^3$$

$$W(z) = \left| \frac{\delta(M(z), \ell(M(z))) - \frac{1}{n(M)} \sum_{z=1}^{z=n(M)} \delta(M(z), \ell(M(z)))}{\sqrt{\left(\frac{1}{n(M)} \sum_{z=1}^{z=n(M)} \delta(M(z), \ell(M(z)))^2 \right) - \left(\frac{1}{n(M)} \sum_{z=1}^{z=n(M)} \delta(M(z), \ell(M(z))) \right)^2}} \right|^3 \quad (9)$$

2.2 Properties of Stego Image

Properties of stego-images (images containing information) depends upon the properties of those pixels in the stego-image which are storing the information. In other words the properties of stego-images become different from the innocent image (image without information) due to deformation produced in certain pixels of stego-image due to embedding of information in those pixels. The basic concepts of steganalysis of Distributing Stego Algorithms is given in Section

3.2 of [7] and the concepts related to steganalysis of Concentrating Stego-Algorithms is given in Section 2.1 of [7] and Section 2.3.1 of [6] (Requirement 3 and Requirement 4).

From [6] and [7] it can be conclusively said that Information pixels (pixels containing hidden information) have following 4 main properties:

1. Since the information pixels are suffering deformations so they are generally quite different from their immediate neighbors. As a result the pixel aberration of information pixels is quite high. Since the concentrating algorithms bring bigger changes in the pixel so Pixel Aberration based analysis is more responsive to the steganalysis of Concentrating Stego-Algorithms.
2. Information has maximum concentration in the LSB Plane of the image. But the LSB Plane of any image appears black and hence its contrast is increased by obtaining the Multicolored LSB Transform of the image. Thus in the Multicolored LSB Transform we can clearly see the information pixels differently colored from the innocent pixels. But since concentrating algorithms change only few pixels and as pixels are very small in size so few counted modified pixels in the Multicolored LSB Plane are imperceptible to human eye and are also statistical point of view are insignificantly less in number. But this method applies perfectly well in steganalysis of Distributing Stego-Algorithms because they modify large number of pixels.
3. In any statistically significant component (50 x 50 pixels) of the Multicolored LSB Plane the distribution of Red, Green and Blue components is significantly unequal among information pixels where as they are nearly equal for innocent pixels. Thus the degree of deviation is more in the information pixels than the innocent pixels.
4. The information pixels are always present in the Fine Grained Pixel Clusters and rarely in the Coarse grained pixel clusters. They are

always absent in the Continuous and Boulder Grained pixels Clusters. Refer Section 3.2 of [7] for details of the classification of pixel clusters. The Multi Color LSB Transform of the images with fine grained pixel clusters have majority of pixel with large value of Pixel Anomaly. Thus the value of the Mean Pixel Anomaly is largest in the fine grained pixel clusters and is lesser in coarse grained and even lesser in boulder grained and least in continuous grained pixel clusters.

2.3 Quantification of the Properties of Stego Image generated by Concentrating Stego Algorithm using Pixel Aberration of the entire Image

These 4 properties associated with the stego-image, can be quantified in to an equivalent numerical values corresponding to the given stego-image. The last three properties are associated with Distributing Stego Algorithms and hence were used in determining Distributing Suspicion Value Λ for any given image in [8]. By using the definitions given in Section 2.1 the first property (related with Pixel Aberration and associated with Concentrating Stego Algorithms) is used for determining the Concentrating Suspicion Value Γ for any given image. Both these numerical values (Λ and Γ) when combined together will be used for determining the holistic Spatial Domain Suspicion Value ζ associated with the image.

2.3.1 Quantification of the Properties Using Weighted Mean Pixel Aberration

Pixel Aberration based analysis responds well to all stego algorithms in general and Concentrating Stego Algorithms in Particular. The concept of Pixel Aberration is based on [6] and [7] and is explained in detail in Definition 6 of Section 2.1 of this paper and mathematically represented in (6) and (7). Since the Pixel Aberration is based on standard deviation so majority of pixels have pixel aberration close to 0. Thus in Definition 7 of Section 2.1 of this paper the pixel aberration for the entire image is calculated by determining the

weighted mean of pixel aberrations of all the pixels in the given image and is mathematically represented in (8) and (9). Thus we examine the performance of Weighted Mean Pixel Aberration as given in (8) and (9) as the measure of Concentrating Suspicion Value Γ for any given image. For this purpose we use two different 100×100 Pixel Images as the cover images. They are represented as A and B and shown in Fig 2. Three different stego algorithms are used for embedding same information (this entire paragraph consisting of 1610 Characters) in all the four images. The first two algorithms are of distributing type (named as Distributing Algorithm 1 and Distributing Algorithm 2) and the third is of Concentrating type. Also the Distributing Algorithm 1 embeds the secret information vertically (Column by Column) and Distributing Algorithm 2 embeds the secret message horizontally (row by row). The three steganographic algorithms used in this paper namely Distributing Algorithm 1, Distributing Algorithm 2 and Concentrating Algorithm were analyzed in [5] and are referred in Section 5 of [5] as *Algorithm designed in section 4*, *QuickStego Software* and *Eureka Steganographer* respectively. The stego-images obtained after inserting information from these three different algorithms are represented as A1, A2, A3 and B1, B2, B3 respectively. Here only A3 and B3 are stego images corresponding to Concentrating Algorithms and rest (A1, A2 and B1, B2) are obtained from Distributing Algorithms.

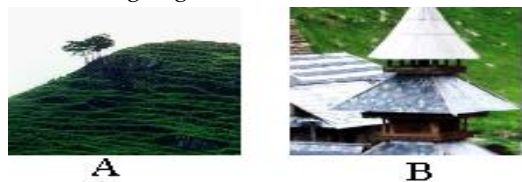


Fig 2 100 x 100 Test Images

The Image B has the properties similar to most other images and hence is a perfect example of a general image but Image A represents a special case of rare occurring images. The Image A is selected because it is one such rare image which has pixel aberration in initial (Row by Row order)

few pixels as almost zero. As a result all other pixels (which do not have Pixel Aberration as absolutely zero) get very high weights causing exceptionally high values of weighted mean pixel aberration for the entire image even though the mean (simple mean) pixel aberration for the pixels of entire image is relatively very low. The same is shown in Table 1 and Table 2. The values of Pixel Aberration for all these eight images (i.e. the Cover Images A and B and the corresponding stego images A1, A2, A3 and B1, B2, B3) are graphically shown in Fig 3. By using (6),(7),(8) and (9) the weighted mean pixel aberration and by using (11) the mean pixel aberration is calculated for all these eight images and the same is tabulated in Table 1 and Table 2 respectively.

Weighted Mean Pixel Aberration for any image M is represented as $\delta_w(M)$ but its value is different for all the three color components red, green and blue and hence the three color components are represented as $\delta_w^R(M)$, $\delta_w^G(M)$ and $\delta_w^B(M)$ respectively. The mean pixel aberration (mean of all the three color components) and Maximum of the three color components represented as $\delta_w^{MEAN}(M)$ and $\delta_w^{MAX}(M)$ respectively is also shown in Table 1. Also $\delta_w^{MAX}(M)$ and $\delta_w^{MEAN}(M)$ is explained mathematically in (10).

$$\begin{aligned}\delta_w^{MAX}(M) &= \text{MAX}(\delta_w^R(M), \delta_w^G(M), \delta_w^B(M)) \\ \delta_w^{MEAN}(M) &= (\delta_w^R(M) + \delta_w^G(M) + \delta_w^B(M))/3.\end{aligned}\tag{10}$$

Also simple mean for any image M is represented by $\delta_m(M)$. Also $\delta_m(M)$ has 3 color components represented as $\delta_m^R(M)$, $\delta_m^G(M)$ and $\delta_m^B(M)$ and also the mean pixel aberration (mean of all the three color components) and Maximum of the three color components represented as $\delta_m^{MEAN}(M)$ and $\delta_m^{MAX}(M)$ respectively.

The values of $\delta_m^R(M)$, $\delta_m^G(M)$ and $\delta_m^B(M)$, $\delta_m^{MAX}(M)$ and $\delta_m^{MEAN}(M)$ for all these eight images is calculated using (11) and tabulated in Table 2.

$$\delta_m(M) = \frac{1}{n(M)} \sum_{z=1}^{z=n(M)} \delta(M(z), \ell(M(z))) \quad (11)$$

From Table 1 and Table 2 we can clearly see that even though the mean pixel aberration of image A is lower than the Image B (Table 2) but still the weighted mean pixel aberration for rare occurring Image A is many times higher (Table 1) than the regular image B (due to distortions in A as explained earlier). Thus we clearly see that determination of the overall pixel aberration by using weighted mean pixel aberration introduces certain unnecessary distortions in few images. Moreover the calculation of weighted pixel aberration requires determination of standard deviation of the pixel aberration for all the pixels of the images and becomes highly complex and time consuming. In fact determination of weighted mean pixel aberration for large images (more than 200 x 200 Pixels) consumes very high computational costs and hangs the program on most occasions. But at the same time relying solely on the simple mean will also not yield a suitable result because for most large images its value becomes insignificantly small. As a remedy a technique based on combination of simple means and weighted means of the pixel aberration for entire image is used for determining the Concentrating Suspicion Value Γ for any given image.

2.3. Quantification of the Properties Using Combination of Simple and Weighted Mean Pixel Aberration for Determination of Concentrating Suspicion Value

There are two different possible approaches of combining simple mean and weighted mean together for calculation of the Concentrating Suspicion Value Γ . Both these approaches are computationally fast because they use a variant of Divide and Conquer Technique and hence break

the entire image into small 5 x 5 to 10 x 10 Pixel Components.

In the first approach the individual simple mean Pixel Aberration for each component is calculated. Using the values of the individual means the overall weighted mean for all the image components together can be calculated as the value of overall Pixel Aberration for any given Image and represented by $\delta_1(M)$ for any Image M . The process of calculating $\delta_1(M)$ for any Image M is explained mathematically in (12). The concentrating suspicion value obtained using Pixel Aberration of any given Image obtained by first approach i.e. $\delta_1(M)$ is represented by $\Gamma_1(M)$ for any given image M .

In second approach the weighted mean pixel aberration is calculated for all the pixels in each component and then an overall simple mean is calculated for weighted mean pixel aberration of each component. Pixel Aberration for any given Image obtained by this approach is represented as $\delta_2(M)$. The process of calculating $\delta_2(M)$ for any Image M is explained mathematically in (13). The concentrating suspicion value obtained using Pixel Aberration of any given Image obtained by second approach i.e. $\delta_2(M)$ is represented by $\Gamma_2(M)$ for any given image M .

2.3.1.1 Concentrating Suspicion Value Calculation by First Approach

The algorithm for calculating the Pixel Aberration for any given Image by combining the Simple and Weighted Means together by First Approach is given in (12). On the basis of (12) the value of $\delta_1(M)$ is calculated for the same images (Fig 2) and shown in Table 3. Since the calculation of $\delta_1(M)$ uses Divide and Conquer technique so its computation is much faster than the calculation of plain weighted mean pixel aberration for entire image i.e. $\delta_w(M)$ as given in (8) and (9). But since the first approach of calculating overall pixel aberration i.e. $\delta_1(M)$ uses weights so even this suffers from the same distortions as the weighted mean pixel aberration $\delta_w(M)$ suffers. But the

magnitude of $\delta_1(\mathbf{M})$ multiplied by 10 is a pretty good indicator of presence of information (stored using concentrating stego algorithms) in any image M and can be considered as the measure of Concentrating Suspicion Value $\Gamma_1(\mathbf{M})$ of image M.

But even more accurate method of determining Concentrating Suspicion Value can be based on the combination of simple mean $\delta_m^{\text{MEAN}}(\mathbf{M})$ and overall Pixel Aberration $\delta_1(\mathbf{M})$. This combination can be done by finding the product of $\delta_m^{\text{MEAN}}(\mathbf{M})$ and $\delta_1(\mathbf{M})$ and can be used as the second measure of concentrating suspicion value $\Gamma_2(\mathbf{M})$ for any image M. Thus the values $\Gamma_1(\mathbf{M})$ and $\Gamma_2(\mathbf{M})$ of Images in Fig 2 is calculated in Table 4 and the algorithm for same is shown in (12). But the second measure of concentrating suspicion value $\Gamma_2(\mathbf{M})$ suffers from much higher complexity and hence consumes far higher computation time and computation power.

2.3.1.2 Concentrating Suspicion Value Calculation by Second Approach

The algorithm for calculating the Pixel Aberration for any given Image by combining the Simple and Weighted Means together by Second Approach is given in (13). On the basis of (13) the value of $\delta_2(\mathbf{M})$ is calculated for the same images (Fig 2) and shown in Table 5. Since the calculation of $\delta_2(\mathbf{M})$ also uses Divide and Conquer Technique so like computation of $\delta_1(\mathbf{M})$ even its computation is much faster than the calculation of plain weighted mean pixel aberration for entire image i.e. $\delta_w(\mathbf{M})$ as given in (8) and (9). In Table 6 we have determined the value of Concentrating Suspicion Value of any Image M represented as $\Gamma_3(\mathbf{M})$ by using second approach based on $\delta_2(\mathbf{M})$ of any image M. The algorithm for calculating $\Gamma_2(\mathbf{M})$ is given in (13).

2.3.2.3 Concentrating Suspicion Value $\Gamma(\mathbf{M})$ (Combining $\Gamma_1(\mathbf{M})$, $\Gamma_2(\mathbf{M})$ and $\Gamma_3(\mathbf{M})$ in to single value)

In Section 2.3.2.1 and Section 2.3.2.2 the Concentrating Suspicion Value of any Image has been calculated by three different methods using (12) and (13) respectively and represented as $\Gamma_1(\mathbf{M})$, $\Gamma_2(\mathbf{M})$ and $\Gamma_3(\mathbf{M})$ respectively. From (12) and (13) it can be clearly concluded that the Complexity

of determining $\Gamma_2(\mathbf{M})$ is far higher than $\Gamma_1(\mathbf{M})$ or $\Gamma_3(\mathbf{M})$. Hence calculation of suspicion value using $\Gamma_2(\mathbf{M})$ is ruled out in all circumstances. The performance of the two different types of concentrating suspicion values $\Gamma_1(\mathbf{M})$ and $\Gamma_3(\mathbf{M})$ is examined by analyzing four different test images acting as cover images and corresponding Stego Images obtained by two different stego softwares. These two softwares are used for embedding same information (1900 Characters) in all the four images as shown in Fig 4. These images (Fig 4) are of dimensions 600x800, 275 x 181, 600 x 800 and 340 x 506 pixels and represented as A, B, C and D respectively. One of the two softwares produces Stego Image by using Distributing Stego Algorithm while the other produces Stego image by using Concentrating Stego Algorithm. The Stego Images produced by Distributing Stego

Table 3

The values of $\delta_1(\mathbf{M})$ of the Cover Images A and B and the corresponding Stego Images

Image M	Description of M	$\delta_1^R(\mathbf{M})$	$\delta_1^G(\mathbf{M})$	$\delta_1^B(\mathbf{M})$	$\delta_1^{\text{MAX}}(\mathbf{M})$	$\delta_1^{\text{MEAN}}(\mathbf{M})$
A	Cover Image (Fig 2, Left)	1.0189	0.4276	0.5924	1.0189	0.6796
A1	Stego (Distributing 1)	3.1412	0.3976	13.2676	13.2676	5.6022
A2	Stego (Distributing 2)	0.9668	0.3965	0.5554	0.9668	0.6396
A3	Stego (Concentrating)	1.3595	1.0443	0.6211	1.3595	1.0083
B	Cover Image (Fig 2, Right)	0.2260	0.2195	0.2324	0.2324	0.2260
B1	Stego (Distributing 1)	0.2354	0.2184	0.2421	0.2421	0.2320
B2	Stego (Distributing 2)	0.2297	0.2186	0.2367	0.2367	0.2283
B3	Stego (Concentrating)	1.2866	1.1435	0.2493	1.2866	0.8931

Table 2

The values of Simple Means of the Cover Images A and B and the corresponding Stego Images

Image M	Description of M	$\delta_m^R(\mathbf{M})$	$\delta_m^G(\mathbf{M})$	$\delta_m^B(\mathbf{M})$	$\delta_m^{\text{MAX}}(\mathbf{M})$	$\delta_m^{\text{MEAN}}(\mathbf{M})$
A	Cover Image (Fig 2, Left)	0.1136	0.1235	0.1045	0.1235	0.1139
A1	Stego (Distributing 1)	0.1298	0.1146	0.1035	0.1298	0.1159
A2	Stego (Distributing 2)	0.1121	0.1294	0.1071	0.1294	0.1162
A3	Stego (Concentrating)	0.1597	0.1601	0.1488	0.1601	0.1562
B	Cover Image (Fig 2, Right)	0.1842	0.1781	0.1742	0.1842	0.1788
B1	Stego (Distributing 1)	0.1823	0.1762	0.1743	0.1823	0.1776
B2	Stego (Distributing 2)	0.1837	0.1767	0.1745	0.1837	0.1783
B3	Stego (Concentrating)	0.2049	0.2053	0.1997	0.2053	0.2033

Table 1
The values of Weighted Means of the Cover Images A and B and the corresponding Stego Images

Image M	Description of M	$\delta_w^R(M)$	$\delta_w^G(M)$	$\delta_w^B(M)$	$\delta_w^{MAX}(M)$	$\delta_w^{MEAN}(M)$	Remarks
A	Cover Image (Fig 2, Left)	18.7204	6.5554	7.9115	18.7204	11.0624	Cover Image has High $\delta_w(M)$. Such images with high value of weighted mean pixel aberration occur rarely.
A1	Stego (Distributing 1)	45.5845	7.6738	218.4825	218.4825	90.5802	
A2	Stego (Distributing 2)	18.1708	5.7362	7.5359	18.1708	10.4809	
A3	Stego (Concentrating)	18.5978	16.4445	16.5742	18.5978	17.2055	
B	Cover Image (Fig 2, Right)	3.7040	4.1700	3.6797	4.1700	3.8512	Cover Image has Low $\delta_w(M)$. It represents commonly occurring general every day image
B1	Stego (Distributing 1)	3.3931	3.4228	3.7255	3.7255	3.5138	
B2	Stego (Distributing 2)	3.6891	4.3328	3.7444	4.3328	3.9221	
B3	Stego (Concentrating)	11.5535	14.1091	31.2673	31.2673	18.9766	

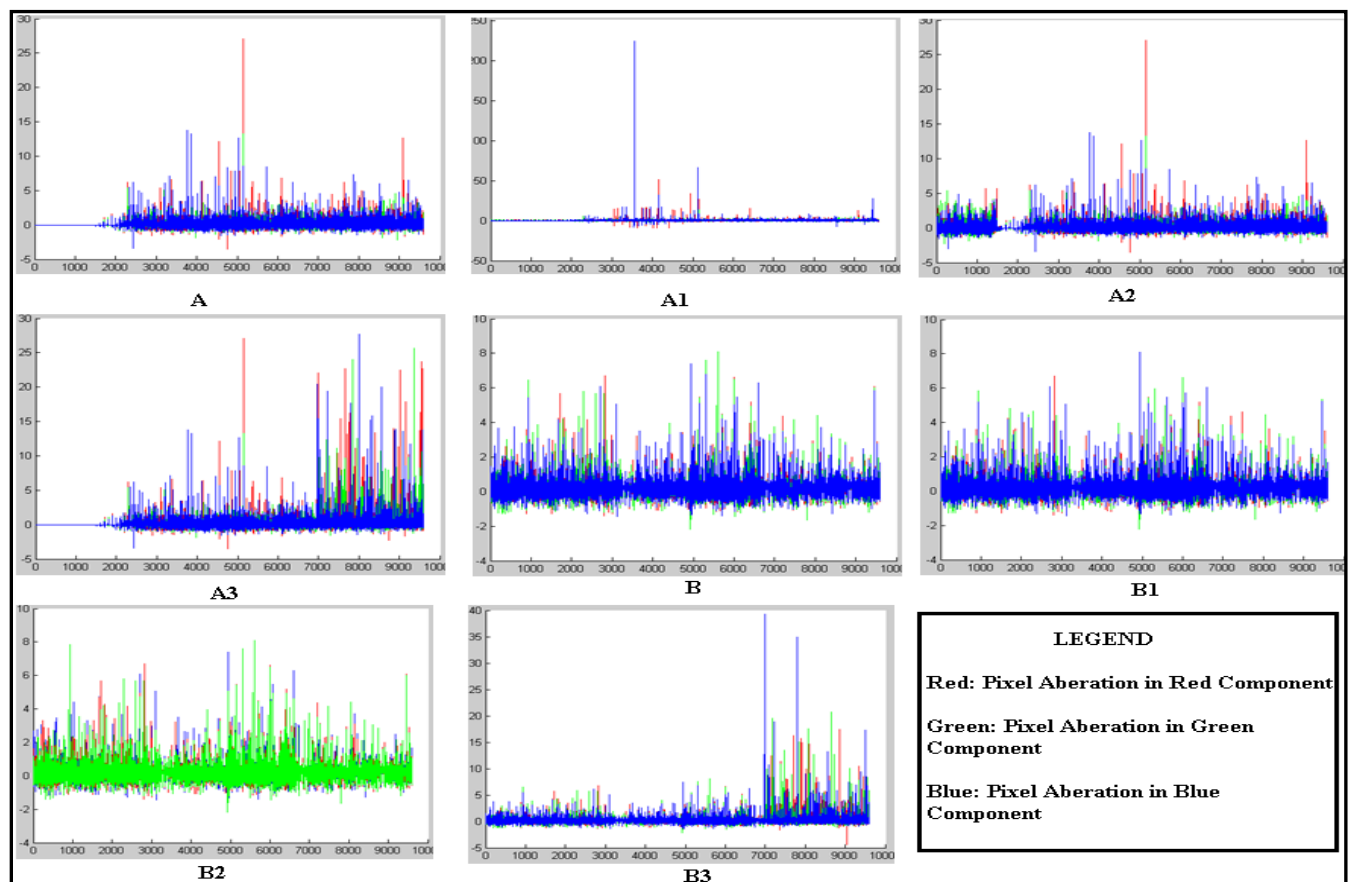


Fig 3 Pixel Aberrations in R,G,B Component of the Cover Image A & B and Corresponding Stego Images A1,A2,A3 & B1,B2,B3

Table 4

The values $\Gamma_1(M)$ and $\Gamma_2(M)$ of the Cover Images A and B and the corresponding Stego Images using $\delta_1(M)$

Image M	Description of M	$\delta_1^{MEAN}(M)$	$\delta_m^{MEAN}(M)$	$\Gamma_1(M) = \delta_1^{MEAN}(M) \times 10$	$\Gamma \delta \delta_m^{MEAN} \delta_1^{MEAN} \delta_2^{MEAN}(M) = \delta_1^{MEAN}(M) \times \delta_m^{MEAN}(M) \times 100$
A	Cover Image (Fig 2, Left)	0.6796	0.1139	6.796	07.7406
A1	Stego (Distributing 1)	5.6022	0.1159	56.022	64.9295
A2	Stego (Distributing 2)	0.6396	0.1162	6.396	07.4322
A3	Stego (Concentrating)	1.0083	0.1562	10.083	15.7496
B	Cover Image (Fig 2, Right)	0.2260	0.1788	2.260	04.0409
B1	Stego (Distributing 1)	0.2320	0.1776	2.320	04.1203
B2	Stego (Distributing 2)	0.2283	0.1783	2.283	04.0706
B3	Stego (Concentrating)	0.8931	0.2033	8.931	18.1567

Table 5

The values of $\delta_2(M)$ of the Cover Images A and B and the corresponding Stego Images

Image M	Description of M	$\delta_2^R(M)$	$\delta_2^G(M)$	$\delta_2^B(M)$	$\delta_2^{MAX}(M)$	$\delta_2^{MEAN}(M)$
A	Cover Image (Fig 2, Left)	1.3362	0.9098	1.3516	1.3516	1.1992
A1	Stego (Distributing 1)	2.2078	1.1126	2.4538	2.4538	1.9247
A2	Stego (Distributing 2)	1.5978	1.1755	1.6106	1.6106	1.4613
A3	Stego (Concentrating)	2.0362	1.5583	1.2786	2.0362	1.6243
B	Cover Image (Fig 2, Right)	1.1592	1.1722	1.1860	1.1860	1.1725
B1	Stego (Distributing 1)	1.1569	1.1500	1.2109	1.2109	1.1726
B2	Stego (Distributing 2)	1.1654	1.1812	1.2072	1.2072	1.1846
B3	Stego (Concentrating)	1.8136	1.9501	1.1279	1.9501	1.6305

Table 6

The values $\Gamma_2(M)$ of Cover Images A and B and the corresponding Stego Images using $\delta_2(M)$

Image M	Description of M	$\delta_2^{MEAN}(M)$	$\Gamma_2(M) = (\delta_2^{MEAN}(M) - 1.2) \times 100$
A	Cover Image (Fig 2, Left)	0.6796	-0.0385
A1	Stego (Distributing 1)	5.6022	36.236
A2	Stego (Distributing 2)	0.6396	13.065
A3	Stego (Concentrating)	1.0083	21.2168
B	Cover Image (Fig 2, Right)	0.2260	-1.3763
B1	Stego (Distributing 1)	0.2320	-1.3684
B2	Stego (Distributing 2)	0.2283	-0.7691
B3	Stego (Concentrating)	0.8931	21.5248

Let the Image to be analyzed be M

The overall Pixel Aberration by First Approach for Image M be $\delta_1(M)$

Let Image M be broken into K Components $M^1, M^2, M^3, \dots, M^K$

Size of Each Image Component is $n(M^i)$

$$\begin{aligned}
 M &= \bigcup_{i=1}^K M^i \\
 \delta_m(M^i) &= \frac{1}{n(M^i)} \sum_{z=1}^{n(M^i)} \delta(M^i(z), \ell(M^i(z))) \\
 \delta_1(M) &= \frac{\sum_{i=1}^K \delta_m(M^i) \times W_i}{\sum_{i=1}^K W_i} \\
 W_i &= \left| \frac{\delta_m(M^i) - \text{MEAN}_{i=1}^K (\delta_m(M^i))}{\text{STD}_{i=1}^K (\delta_m(M^i))} \right|^3 \\
 \text{OR} \\
 W_i &= \left| \frac{\delta_m(M^i) - \frac{1}{K} \sum_{i=1}^K \delta_m(M^i)}{\sqrt{\frac{1}{K} \left(\sum_{i=1}^K (\delta_m(M^i) - \frac{1}{K} \sum_{i=1}^K \delta_m(M^i))^2 \right)}} \right|^3 \\
 \Gamma_1(M) &= \delta_1(M) \times 10 = \frac{\sum_{i=1}^K \delta_m(M^i) \times W_i}{\sum_{i=1}^K W_i} \times 10 \\
 \Gamma_2(M) &= \frac{\delta_m(M)}{\delta_1(M)} \times 100 \\
 &= \frac{1}{n(M)} \sum_{z=1}^{n(M)} \delta(M(z), \ell(M(z))) \times \frac{\sum_{i=1}^K \delta_m(M^i) \times W_i}{\sum_{i=1}^K W_i} \times 100
 \end{aligned}$$

(12)

Let the Image to be analyzed be M

The overall Pixel Aberration of Image M be $\delta(M)$

Let Image M be broken into K Components $M^1, M^2, M^3, \dots, M^K$

Size of Each Image Component is $n(M^i)$

$$M = \bigcup_{\substack{i=1 \\ M^i \subset M}}^K M^i$$

$$\delta_w(M^i) = \frac{\sum_{\substack{z=1 \\ M^i(z) \in M^i \\ M^i \subset M}}^{n(M^i)} |\delta(M^i(z), \ell(M^i(z)))| \times W^i(z)}{\sum_{\substack{z=1 \\ M(z) \in M}}^N W^i(z)}$$

$$W_i(z) = \left| \frac{\delta(M^i(z), \ell(M^i(z))) - \text{MEAN}_{i=1}^K (\delta(M^i(z), \ell(M^i(z))))}{\text{STD}_{i=1}^K (\delta(M^i(z), \ell(M^i(z))))} \right|^3$$

OR

$$W_i(z) = \left| \frac{\delta(M^i(z), \ell(M^i(z))) - \frac{1}{n(M^i)} \sum_{\substack{z=1 \\ M^i(z) \in M^i \\ M^i \subset M}}^{n(M^i)} \delta(M^i(z), \ell(M^i(z)))}{\sqrt{\left(\frac{1}{n(M^i)} \sum_{\substack{z=1 \\ M^i(z) \in M^i \\ M^i \subset M}}^{n(M^i)} \delta(M^i(z), \ell(M^i(z)))^2 \right) - \left(\frac{1}{n(M^i)} \sum_{\substack{z=1 \\ M^i(z) \in M^i \\ M^i \subset M}}^{n(M^i)} \delta(M^i(z), \ell(M^i(z))) \right)^2}} \right|^3$$

$$\delta_2(M) = \frac{1}{K} \sum_{\substack{i=1 \\ M^i \subset M}}^K \delta_w(M^i)$$

$$\Gamma_3(M) = (\delta_2(M) \cdot 1.2) \times 100$$

(13)

Algorithms are represented as A_d ,B_d ,C_d and D_d while the Stego Images produced by Concentrating Stego Algorithms are represented as A_c, B_c, C_c and D_c.

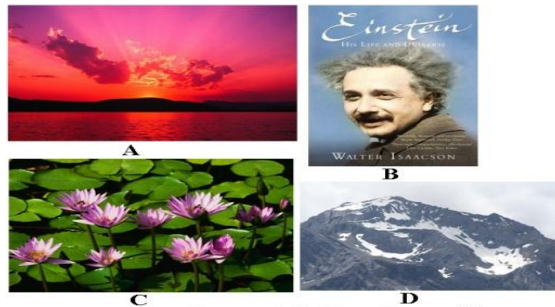


Fig 4 Test Images A,B,C and D used for determination of $\Gamma(M)$, $\zeta(M)$ and $\Lambda(M)$

Table 7

The Values of $\Gamma_1(M)$, $\Gamma_3(M)$ and $\Gamma(M)$ of four different Cover Images (A,B,C and D) and the corresponding Stego Images

Image M	Image Properties	$\Gamma_1(M)$	$\Gamma_3(M)$	$\Gamma(M) = \text{MAX}(\Gamma_1(M), \Gamma_3(M))$
A	600x800 Pixel Cover	2.192	-17.3155	2.192
A_d	Distributing	2.1966	-16.0829	2.1966
A_c	Concentrating	20.3353	-6.0160	20.3353
B	275x181 Pixel Cover	4.5153	-12.1805	4.5153
B_d	Distributing	4.5346	-10.389	4.5346
B_c	Concentrating	261.0982	184.8828	261.0982
C	600x800 Pixel Cover	1.909	-25.7871	1.909
C_d	Distributing	1.9708	-24.4523	1.9708
C_c	Concentrating	53.8520	-12.9077	53.8520
D	340x506 Pixel Cover	2.8924	-4.6067	2.8924
D_d	Distributing	2.9313	-4.2348	2.9313
D_c	Concentrating	20.0985	-1.9733	20.0985

From Table 7 it can be easily concluded that $\Gamma_3(M)$ is the true measure of Concentrating Suspicion Value $\Gamma(M)$ of any Image M. The same can be mathematically written as $\Gamma(M) = \Gamma_3(M)$.

2.4 Determination of Overall Suspicion Value ζ

The values of Concentrating Suspicion Value $\Gamma(M)$ as obtained from Table 7 is combined with the Distributing Suspicion Value $\Lambda(M)$ (determined from (17) in [8]) to Produce Overall Suspicion Values $\zeta(M)$ for the four different test images in Fig 4 (A,B,C and D) and the corresponding Stego Images (A_d, B_d, C_d and D_d; A_c, B_c, C_c and D_c). The same is shown in Table 8. Thus we see

that Overall Suspicion Value $\zeta(M)$ is very much higher for all the images having hidden information while it is much lower for the innocent cover images. The Overall Suspicion Value $\zeta(M)$ for any image M is the maximum of the Concentrating and Distributing Suspicion Values and mathematically given in (14).

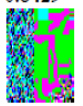
$$\zeta(M) = \text{MAX}(\Gamma(M), \Lambda(M)) \quad (14)$$

3 CONCLUSION

The Distributing Suspicion Value (obtained from (17) in [8]) and Concentrating Suspicion Value (obtained from (12), (13) and (14)) are combined together using (15) to produce Overall Suspicion Value $\zeta(M)$ associated with any given image M. From Table 8 it can be clearly seen that this numerical quantifier $\zeta(M)$ is higher for all those images which have some information embedded in them while it is much lower for all innocent cover images. Hence this holistic suspicion value $\zeta(M)$ (which applies on both the Concentrating as well as Distributing Stego Algorithms) is a quick identifier of presence of information in any given image and can be effectively used as Stego Identifier Algorithm. This fast stego-identification technique will find its application in quick filtering of the suspicious images flowing through the web servers, routers, layer three switches and all other electronic media concerned with transmission of images and will be very useful tool against terrorists and all other malafide cyber networks.

Table 8

The Values of $\Gamma(M)$, $\Lambda(M)$ and $\zeta(M)$ of four different Cover Images (A, B, C and D) and the corresponding Stego Images

Image M	Image Properties	$\Gamma(M)$	$\Lambda(M)$	$\zeta(M) = \text{MAX}(\Gamma(M), \Lambda(M))$
A	600x800 Pixel Cover	2.192	3.0581	3.0581
A_d	Distributing	2.1966	43.9658	43.9658
A_c	Concentrating	20.3353	3.0558	20.3353
B	275x181 Pixel Cover	4.5153	2.1899	4.5153
B_d	Distributing	4.5346	17.9565	17.9565
B_c	Concentrating	261.0982	2.1899	261.0982
C	600x800 Pixel Cover	1.909	3.2240	3.2240
C_d	Distributing	1.9708	34.3697	34.3697
C_c	Concentrating	53.8520	3.2858	53.8520
D	340x506 Pixel Cover	2.8924	1.2039	2.8924
D_d	Distributing	2.9313	0.8429	 Ambiguous Section when analyzed in detail clearly shows the presence of information embedded in those sections.
D_c	Concentrating	20.0985	1.2039	

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